

GUJARAT TECHNOLOGICAL UNIVERSITY**B.VOC- SEMESTER– II EXAMINATION – WINTER 2023****Subject Code:21120204****Date:01-01-2024****Subject Name:Basic Mathematics****Time:02:30 PM TO 04:30 PM****Total Marks:50****Instructions:**

1. Attempt all questions.
2. Make suitable assumptions wherever necessary.
3. Figures to the right indicate full marks.
4. Simple and non-programmable scientific calculators are allowed.

- | | | Marks | | | | | | | | | | | | | | | | | | | | | | |
|-----------|--|--------------|-------|-------|-------|-------|-------|-------|-----------|----|----|----|-----|----|----|----|-----|-----|----|----|----|----|----|--|
| Q1 | (a) If $A = \{1, 2, 3, 4\}$, $B = \{3, 4, 9, 11\}$ and $C = \{2, 11, 18, 22\}$ then verify that
$A \cup (B \cap C) = (A \cup B) \cap (A \cup C)$ | 05 | | | | | | | | | | | | | | | | | | | | | | |
| | (b) Define Graph and multiple edges with example | 05 | | | | | | | | | | | | | | | | | | | | | | |
| Q2 | (a) Solve the equation $6x^2 - 5x = 4$. | 05 | | | | | | | | | | | | | | | | | | | | | | |
| | (b) Find real and imaginary part of $\frac{1+2i}{1-3i}$. | 05 | | | | | | | | | | | | | | | | | | | | | | |
| | OR | | | | | | | | | | | | | | | | | | | | | | | |
| | (b) Let $f: A \rightarrow B$ where $A = \{1, 2, 3\}$; $B = \{1, 2, 3, 4, 5, 6, 7, 8, 9\}$ $f(x) = x^2$ then find domain, co-domain and range of f . | 05 | | | | | | | | | | | | | | | | | | | | | | |
| Q3 | (a) Let $u = (1, 2, 3)$ and $v = (2, -3, 7)$. Then find $u + v$, $3u$, $-2v$, $3u - 2v$, $u \cdot v$ | 05 | | | | | | | | | | | | | | | | | | | | | | |
| | (b) If $\begin{vmatrix} 2 & 3 \\ 4 & 5 \end{vmatrix} = \begin{vmatrix} x & 3 \\ 2x & 5 \end{vmatrix}$ then find the value of x | 05 | | | | | | | | | | | | | | | | | | | | | | |
| | OR | | | | | | | | | | | | | | | | | | | | | | | |
| Q3 | (a) Define Relation. Explain different types of relation with examples. | 05 | | | | | | | | | | | | | | | | | | | | | | |
| | (b) If $A = \begin{bmatrix} 1 & -2 & 3 \\ 0 & 4 & 5 \end{bmatrix}$ and $B = \begin{bmatrix} 4 & 6 & 8 \\ 1 & -3 & -7 \end{bmatrix}$ then find $A + B$, $3A$, $2A - 3B$ | 05 | | | | | | | | | | | | | | | | | | | | | | |
| Q4 | (a) Find mean deviation of the following data | 05 | | | | | | | | | | | | | | | | | | | | | | |
| | <table border="1" style="width: 100%; border-collapse: collapse; text-align: center;"> <tr> <td>x</td><td>5</td><td>6</td><td>7</td><td>8</td><td>9</td><td>10</td><td>11</td><td>12</td><td>13</td><td>14</td> </tr> <tr> <td>f</td><td>25</td><td>45</td><td>90</td><td>165</td><td>112</td><td>96</td><td>81</td><td>26</td><td>18</td><td>12</td> </tr> </table> | x | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 | 13 | 14 | f | 25 | 45 | 90 | 165 | 112 | 96 | 81 | 26 | 18 | 12 | |
| x | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 | 13 | 14 | | | | | | | | | | | | | | |
| f | 25 | 45 | 90 | 165 | 112 | 96 | 81 | 26 | 18 | 12 | | | | | | | | | | | | | | |
| | (b) A card is drawn from a well-shuffled pack of 52 cards. Find the probability of
(i) getting a king card (ii) getting a red card | 05 | | | | | | | | | | | | | | | | | | | | | | |
| | OR | | | | | | | | | | | | | | | | | | | | | | | |
| Q4 | (a) Find the quartile deviation from the following data: | 05 | | | | | | | | | | | | | | | | | | | | | | |
| | <table border="1" style="width: 100%; border-collapse: collapse; text-align: center;"> <tr> <td>Class</td><td>0-5</td><td>5-10</td><td>10-15</td><td>15-20</td><td>20-25</td><td>25-30</td> </tr> <tr> <td>Frequency</td><td>4</td><td>6</td><td>8</td><td>12</td><td>7</td><td>2</td> </tr> </table> | Class | 0-5 | 5-10 | 10-15 | 15-20 | 20-25 | 25-30 | Frequency | 4 | 6 | 8 | 12 | 7 | 2 | | | | | | | | | |
| Class | 0-5 | 5-10 | 10-15 | 15-20 | 20-25 | 25-30 | | | | | | | | | | | | | | | | | | |
| Frequency | 4 | 6 | 8 | 12 | 7 | 2 | | | | | | | | | | | | | | | | | | |
| | (b) If A and B are two events such that $P(A) = 0.3$, $P(B) = 0.4$ and $P(A \cap B) = 0.2$, find (i) $P(A \cup B)$ (ii) $P(\bar{A})$ (iii) $P(\bar{B})$ (iv) $P(\bar{A} \cap B)$ (v) $P(\bar{A} \cup \bar{B})$ | 05 | | | | | | | | | | | | | | | | | | | | | | |
| Q5 | (a) Construct truth table for $A \wedge (B \vee C) \leftrightarrow (A \wedge B) \vee (A \wedge C)$ | 05 | | | | | | | | | | | | | | | | | | | | | | |
| | (b) Explain different types of logic gate with diagram | 05 | | | | | | | | | | | | | | | | | | | | | | |

OR

- Q5** (a) State De Morgan's Law and prove it using truth table **05**
(b) Design a Boolean function of $A \oplus B + C'$ using logic gates **05**
