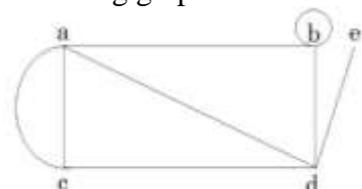


GUJARAT TECHNOLOGICAL UNIVERSITY**B.VOC- SEMESTER-II EXAMINATION – SUMMER 2022****Subject Code:21120204****Date:02-08-2022****Subject Name:Basic Mathematics****Time:10:30 AM TO 12:30 PM****Total Marks:50****Instructions:**

1. Attempt all questions.
2. Make suitable assumptions wherever necessary.
3. Figures to the right indicate full marks.
4. Simple and non-programmable scientific calculators are allowed.

- Q.1** (a) If $A = \{1,2,3,4\}$, $B = \{3,4,9,11\}$ and $C = \{2,11,18,22\}$ then find **Marks 05**
 (i) $(A \cap B)$, (ii) $(B \cap C)$, (iii) $(A \cap C)$, (iii) $(A \cap B \cap C)$.
- (b) Find edges, vertices, parallel edges, loops, degree of vertices from the following graph **05**



- Q.2** (a) Solve the equation $3x^2 + 5x = 2$. **05**
- (b) Find real and imaginary part of $\frac{3-4i}{5+7i}$. **05**

OR

- (b) Let $f: A \rightarrow B$ where $A = \{1,2,3\}$; $B = \{1,2,3,4,5,6,7\}$
 $f(x) = 2x$ then find domain, co-domain and range of f . **05**
- Q.3** (a) Let $u = (2, 3, -4)$ and $v = (1, -5, 8)$. Then find $u + v$, $5u$, $-v$, $2u - 3v$, $u \cdot v$ **05**
- (b) If $\begin{vmatrix} 11 & 40 & 28 \\ 3 & 12 & 8 \\ a & 2 & 2 \end{vmatrix} = 0$ Then find a **05**

OR

- Q.3** (a) Consider the following relation on $\{1, 2, 3, 4, 5, 6\}$ $R = \{(i, j) : |i - j| = 2\}$ **05**
 . Is R reflexive, symmetric or transitive ?
- (b) Find AB and BA , where $A = \begin{bmatrix} 1 & -1 & 1 \\ -3 & 2 & -1 \\ -2 & 1 & 0 \end{bmatrix}$, $B = \begin{bmatrix} 1 & 2 & 3 \\ 2 & 4 & 6 \\ 1 & 2 & 3 \end{bmatrix}$ **05**

- Q.4** (a) Find standard deviation of the following data **05**
- | | | | | | | | | | |
|-----|----|----|----|----|----|----|----|----|----|
| x | 10 | 11 | 12 | 13 | 14 | 15 | 16 | 17 | 18 |
| f | 2 | 7 | 10 | 12 | 15 | 11 | 10 | 6 | 3 |
- (b) Three unbiased coins are tossed. Find the probability of getting (i) exactly two heads (ii) atleast one tail **05**

OR

- Q.4** (a) Find the quartile deviation from the following data: **05**
- | | | | | | | | | |
|-----------|------|-------|-------|-------|-------|-------|-------|-------|
| Class | 5-10 | 10-15 | 15-20 | 20-25 | 25-30 | 30-35 | 35-40 | 40-45 |
| Frequency | 5 | 6 | 15 | 10 | 5 | 4 | 2 | 3 |

- (b) If A and B are two events such that $P(A)=0.3$, $P(B)=0.4$ and $P(A \cap B)=0.2$, find (i) $P(A \cup B)$ (ii) $P(\bar{A})$ (iii) $P(\bar{B})$ (iv) $P(\bar{A} \cup B)$ (v) $P(\bar{A} \cap \bar{B})$ **05**

Q.5 (a) State De Morgan's Law and prove it using postulates **05**

(b) Check whether F_2 is a minimization of F_1 , where, **05**

$$F_1 = \bar{x} \cdot \bar{y} \cdot z + \bar{x} \cdot y \cdot z + \bar{x} \cdot y \text{ and } F_2 = x \cdot \bar{y} + \bar{x} \cdot z.$$

OR

Q.5 (a) Use truth table to prove that **05**

$$(A + B) \cdot (A + C) = A + (B \cdot C)$$

(b) Design a Boolean function of $AB + CD$ using logic gates **05**
