

GUJARAT TECHNOLOGICAL UNIVERSITY**BE - SEMESTER-IV (NEW) EXAMINATION – SUMMER 2021****Subject Code:2140706****Date:06/09/2021****Subject Name:Numerical and Statistical Methods for Computer Engineering****Time:02:30 PM TO 05:00 PM****Total Marks:70****Instructions:**

1. Attempt all questions.
2. Make suitable assumptions wherever necessary.
3. Figures to the right indicate full marks.
4. Simple and non-programmable scientific calculators are allowed.

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|------------|---|-----------|
| Q.1 | (a) For $a = 3.141592$ and approximate value of a as 3.14 evaluate absolute error, relative error, and percentage error. | 03 |
| | (b) Find a root of $x^3 - 5x + 3 = 0$ by the bisection method correct up to four decimal places. | 04 |
| | (c) Derive the iteration formula for \sqrt{N} and hence, find $\sqrt{65}$. | 07 |
| Q.2 | (a) Solve the following system of equations:
$x + 3y + 2z = 5$
$2x + 4y - 6z = -4$
$x + 5y + 3z = 10$ | 03 |
| | (b) Solve the following systems of equations using partial pivoting by the Gauss elimination method.
$2x + 3y + x = 6$
$4x + 2y + 3z = 4$
$4x + y + z = 0$ | 04 |
| | (c) Solve the following systems of equations using Gauss Jacobi method.
$6x + 2y - z = 4$
$X + 5y + 4z = 27$ | 07 |

OR

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|------------|--|-----------|
| Q.3 | (c) Use the Gauss-Seidal method to solve
$6x + y + z = 105$
$4x + 8y + 3z = 155$
$5x + 4y - 10z = 65$ | 07 |
| | (a) Write relation between Δ and E , ∇ and E . | 03 |
| | (b) Determine the polynomial by Newton's forward difference formula from the following table. | 04 |

x	0	1	2	3	4	5
y	-10	-8	-8	-4	10	40

- | | | |
|------------|--|-----------|
| Q.3 | (c) Employ Stirling's formula to compute $y(35)$ from the following table. | 07 |
|------------|--|-----------|

x	20	30	40	50
y	512	439	346	243

OR

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|------------|--|-----------|
| Q.3 | (a) Write relation between δ and E , μ and E . | 03 |
| | (b) Using Lagrange's interpolation formula, find the value of y when $x = 10$ from the following table | 04 |
| | (c) Using Newton's divided differences formula, compute $f(0.5)$ from the following table. | 07 |

X	5	6	9	11
Y	12	13	14	16

X	10	11	13	17
F(x)	2.3026	2.3989	2.5649	2.8332

Q.4 (a) Fit a straight line to the following data. **03**

X	1	2	3	4	6	8
Y	2.4	3	3.6	4	5	6

(b) State Trapezoidal rule with $n = 10$ and evaluate $\int_0^1 e^x dx$. **04**

(c) Find the value y for $y' = x + y$, $y(0) = 1$ when $x = 0.1, 0.2$ with step size $h = 0.05$. **07**

OR

Q.4 (a) Fit a straight line to the following data. **03**

X	0	1	2	3	4
Y	1	1.8	3.3	4.5	6.3

(b) Using Simpsons 1/3 rule with $n = 10$ and evaluate $\int_0^1 e^x dx$. **04**

(c) Given that $y = 1.3$ and $x = 1$, and $y' = 3x + y$. Use the second order Runge- Kutta method to approximate y when $x = 1.2$. Use step size of $x = 0.1$. **07**

Q.5 (a) Calculate the mean for the following frequency distribution. **03**

Class	0-8	8-16	16-24	24-32	32-40	40-48
Frequency	8	7	16	24	15	7

(b) Calculate the first four movement of the following data. **04**

X	0	1	2	3	4	5	6	7	8
F	5	10	15	20	25	30	15	10	5

(c) Calculate the regression coefficient and find two line of regression from the following data. **07**

X	57	58	59	59	60	61	62	64
Y	67	68	65	68	72	72	69	71

OR

Q.5 (a) Calculate the arithmetic mean of the following marks obtained by students **03**

(b) Find the first four movements of the following data about the assumed mean 25 and actual mean. **04**

Class limit	0-10	10-20	20-30	30-40
Frequency	1	3	4	2

(c) Following data represents rainfall (x) and yield of paddy per hectare (y) in a particular area. Find the linear regression of x on y . **07**

X	113	102	95	120	140	130	125
Y	1.8	1.5	1.3	1.9	1.1	2.0	1.7
