

Seat No.: _____

Enrolment No. _____

GUJARAT TECHNOLOGICAL UNIVERSITY

BE - SEMESTER-VI(OLD) – EXAMINATION – SUMMER 2019

Subject Code:160704

Date:18/05/2019

Subject Name: Theory Of Computation

Time:10:30 AM TO 01:00 PM

Total Marks: 70

Instructions:

1. Attempt all questions.
2. Make suitable assumptions wherever necessary.
3. Figures to the right indicate full marks.

Q.1 (a) Write Principle of Mathematical Induction. Using Principle of Mathematical Induction, prove that for every $n \geq 1$, **07**

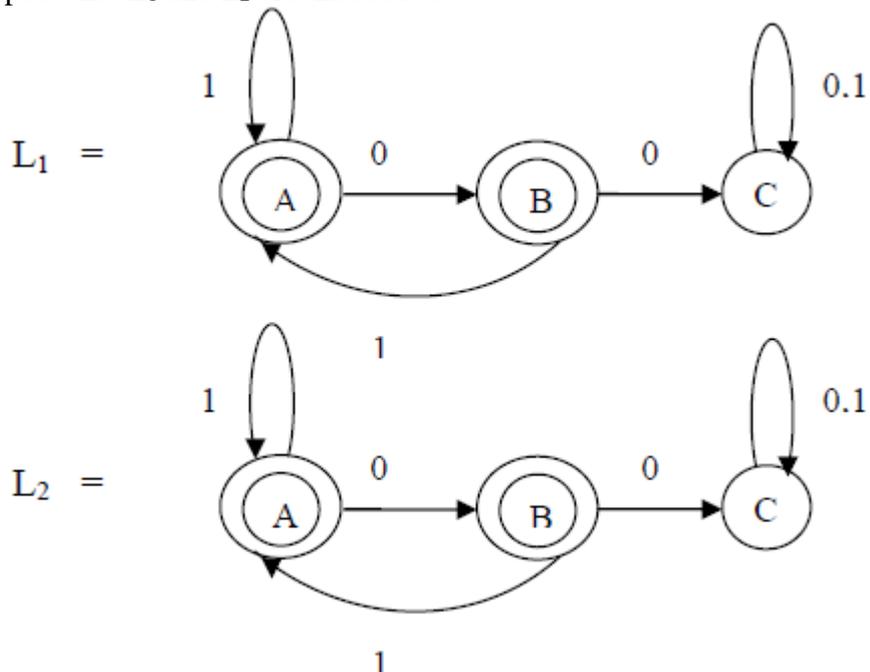
$$\sum_{i=1}^n i^2 = \frac{n(n+1)(2n+1)}{6}$$

(b) Define reflexivity, symmetry, and transitivity properties of relations. Consider the relation $R = \{(1,2), (1,1), (2,1), (2,2), (3,2), (3,3)\}$ defined over $\{1, 2, 3\}$. Is it reflexive? Symmetric? Transitive? Justify each of your answers. **07**

Q.2 (a) Convert NFA- \wedge to NFA and DFA. Initial State: A, Final State : D **07**

Q	$\delta(q, \wedge)$	$\delta(q, 0)$	$\delta(q, 1)$
A	{B}	{A}	ϕ
B	{D}	{C}	ϕ
C	ϕ	ϕ	{B}
D	Φ	{D}	ϕ

(b) Suppose that L_1 and L_2 are the subsets **07**



Draw the FAs recognizing the following Languages:

- $L_1 \cap L_2$
- $L_1 - L_2$

OR

- (b) Define Pumping Lemma for Regular Languages. Use Pumping Lemma to show that the following languages are not regular. **07**

$$L = \{ 0^n 1^{2n} \mid n > 0 \}$$

$$L = \{ ww^R \mid w \in \{0,1\}^* \}$$

- Q.3** (a) Define Ambiguous grammar. Write Unambiguous grammar for following grammar : **07**

$$E \rightarrow E + E \mid E * E \mid (E) \mid id$$

Derive string "id+id*id" using unambiguous grammar.

- (b) Given the CFG G, find a CFG G' in Chomsky Normal form generating $L(G) - \{ \Lambda \}$ **07**

$$S \rightarrow A \mid B \mid C$$

$$A \rightarrow aAa \mid B$$

$$B \rightarrow bB \mid bb$$

$$C \rightarrow aCaa \mid D$$

$$D \rightarrow baD \mid abD \mid aa$$

OR

- (a) Design Context Free Grammar for following Language : **07**

$$L = \{ 0^i 1^j 0^k \mid j > i + k \}$$

- (b) Write Regular Expressions corresponding to each of the following subsets of $\{0,1\}^*$ **07**

(i) The language of all strings in $\{0,1\}^*$ that containing at least two 0's.

(ii) The language of all strings containing both 101 and 010 as substrings.

(iii) The language of all strings that do not end with 01.

- Q.4** (a) Design PDA for the language $L = \{ x \in \{a, b\}^* \mid n_a(x) > n_b(x) \}$. **07**

- (b) Explain Cook's Theorem. **07**

OR

- (a) Design PDA for the language $L = \{ xcx^r \mid x \in \{a, b\}^* \}$ **07**

- (b) Write Short note on Any Two : **07**

(i) The Primitive Recursion Function

(ii) P and NP Completeness

(iii) Equivalence Relation

- Q.5** (a) Design Turing Machine(TM) to accept Palindrome over $\{a,b\}$, even as well as odd. **07**

- (b) Write Short note on Following: **07**

(i) Halting Problem

(ii) Church Turing Thesis

OR

- (a) Design Turing Machine to copy string. **07**

- (b) Explain Time Complexity and Space Complexity. **07**
